

Generation Rules

$$\begin{array}{c}
\frac{x :_\lambda \tau \in \Gamma}{\Gamma \vdash x : \tau \rightsquigarrow \epsilon} \text{VARCON}_\lambda \\
\\
\frac{\alpha \text{ fresh} \quad x : \sigma \in \Gamma}{\Gamma \vdash x : \alpha \rightsquigarrow \text{InstanceOf}(\sigma, \alpha)} \text{VARCON} \\
\\
\frac{\alpha \text{ fresh} \quad \Gamma, x :_\lambda \alpha \vdash e : \tau \rightsquigarrow C}{\Gamma \vdash \lambda x. e : \alpha \rightarrow \tau \rightsquigarrow C} \text{ABS} \\
\\
\frac{\Gamma, x : \sigma_1 \vdash e : \tau_2 \rightsquigarrow C}{\Gamma \vdash \lambda(x :: \sigma_1). e : \sigma_1 \rightarrow \tau_2 \rightsquigarrow C} \text{ABSA} \\
\\
\frac{\Gamma \vdash e_1 : \tau_1 \rightsquigarrow C_1 \quad \Gamma \vdash e_2 : \tau_2 \rightsquigarrow C_2 \quad \alpha \text{ fresh}}{\Gamma \vdash e_1 e_2 : \alpha \rightsquigarrow C_1 \wedge C_2 \wedge \tau_1 \sim \tau_2 \rightarrow \alpha} \text{APP} \\
\\
\frac{\Gamma \vdash e : \tau_2 \rightsquigarrow C}{\Gamma \vdash (e :: \sigma_1) : \sigma_1 \rightsquigarrow C \wedge \text{InstanceOf}(\tau_2, \sigma_1)} \text{ANNOT} \\
\\
\frac{\Gamma \vdash e_1 : \tau_1 \rightsquigarrow C_1 \quad \Gamma, x :_\lambda \tau_1 \vdash e_2 : \tau_2 \rightsquigarrow C_2}{\Gamma \vdash \text{let } x = e_1 \text{ in } e_2 : \tau_2 \rightsquigarrow C_1 \wedge C_2} \text{LET} \\
\\
\frac{\Gamma, x : \sigma_1 \vdash e_1 : \sigma_1 \rightsquigarrow C_1 \quad \Gamma, x : \sigma_1 \vdash e_2 : \tau_2 \rightsquigarrow C_2}{\Gamma \vdash \text{let } x :: \sigma_1 = e_1 \text{ in } e_2 : \tau_2 \rightsquigarrow C_1 \wedge C_2} \text{LETA} \\
\\
\begin{array}{c}
\Gamma \vdash e : \tau \rightsquigarrow C \\
\text{for each branch } K_i \bar{x}_i \rightarrow u_i \text{ do} \\
K_i : \forall \bar{a} \bar{b}_i. Q_i \Rightarrow \bar{v}_i \rightarrow \top \bar{a} \in \Gamma \quad \bar{b}_i \text{ fresh} \\
\Gamma, x_i : [\bar{a} \mapsto \bar{\gamma}] \bar{v}_i \vdash u_i : \tau_i \rightsquigarrow C_i \\
\bar{\delta}_i = fuv(\tau_i, C_i) - fuv(\Gamma, \bar{\gamma}) \\
C'_i = \begin{cases} C_i \wedge \tau_i \sim \beta & \text{if } \bar{b}_i \text{ and } Q_i \text{ empty} \\ \forall \bar{\delta}_i. ([\bar{a} \mapsto \bar{\gamma}]) Q_i \supset C_i \wedge \tau_i \sim \beta \end{cases} \\
\hline
\Gamma \vdash \text{case } e \text{ of } \{K_i \bar{x}_i \rightarrow u_i\} : \beta \rightsquigarrow C \wedge \top \bar{\gamma} \sim \tau \wedge \bigwedge C'_i \text{ CASE}
\end{array}
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